# Four-Quadrant Chopper for Two DC Motor Drives of Electric Wheelchair

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This paper presents a newly designed chopper circuits and its operation that can drive two DC motors at the same time, which is applied to an electric wheelchair system. By using the new topology, the switching devices count can be reduced. By some simulated and experimental results, the operation of the new topology circuit is examined in detail. As a result, it is cleared that the chopper circuit has satisfied performance for driving two DC motors.

(Keywords, chopper, DC motor, electric wheelchair)

#### 1. Introduction

The authors have been developing the electric wheelchair using PEM fuel cell <sup>(1)-(3)</sup>. Because of the limitation of energy used in the electric wheelchair system, the DC motor drive circuit much be designed to save energy as much as possible. Moreover, for commercial application, a low cost of DC chopper is considered. The electric wheelchair using fuel cell has been proposed in Ref. (5) but their system still use the conventional DC chopper for motor drive circuit. According to the DC motor drives circuit, a newly designed DC chopper has been proposed. However, it has some disadvantages point such as the maximum output voltage of chopper circuit cannot be achieved.

Therefore, this paper proposes a novel chopper circuit and its operation capable to drive two DC motors at the same time, which is mainly applied to an electric wheelchair drive. The key feature of the proposed circuit is reduced counts of the switching devices without sacrificing a perfectly independent four-quadrant operation and a voltage boost operation of a power source. Several experimental results are presented to confirm proper operations of the proposed circuit.

## 2. Circuit Configuration

The conventional four-quadrant H-bridge DC chopper is shown in Fig. 1. This circuit topology is widely used in various applications. One of them is to use as a DC chopper for the four-quadrant control in a DC machine<sup>(4)</sup>. In the circuit topology, one set of DC motor requires 4 switching devices to operate in four-quadrant operation. If the system has two DC motor such as the electric wheelchair system, therefore, 8 switching devices are required to operate these motor. Fig. 2 shows a three-leg structure based full-bridge chopper to drive independent two DC motors simultaneously.

In the circuit, a center leg composed with  $Q_3$  and  $Q_4$  is operated at a relatively low-frequency, e. g., 1 kHz, while the other two legs composed with  $Q_1$ ,  $Q_2$ ,  $Q_5$  and  $Q_6$  are operated at a frequency approximately ten times of the center leg. The switching operation of  $Q_3$  and  $Q_4$  is complementary with a 50-% duty cycle; hence the proposed chopper allows independent drive of the two DC motors in four-quadrant operation similar to the conventional topology.



Fig. 1. Conventional four-quadrant H-bridge DC chopper.







Fig. 3. Proposed three-leg full-bridge chopper incorporated voltage boost function.

However, the 50-% duty cycle switching operation of  $Q_3$ and  $Q_4$  limits the chopper output voltages to half of the power source. Assuming that a 200-W, 24-V battery is a power supply, the maximum voltages across the two DC motors are limited to 12 V, which implies that the maximum speed of the motors is reduced to half of the inherent rated value. Inserting a boost circuit between the power source and the three-leg full-bridge chopper may solve this problem, resulting in increase of the switching device counts and complexity of the circuit configuration. A novel approach to solve the above drawback is presented in Fig. 3. The two DC motors are driven by the three-leg full-bridge chopper, which is composed with superimposed two full-bridge choppers at The total number of the switching the center leg. devices is reduced to six. The switching frequency of  $Q_1$ ,  $Q_2$ ,  $Q_5$  and  $Q_6$  is 10 kHz, while that of  $Q_3$  and  $Q_4$  is set at 1 kHz.

The most significant point of this configuration is a voltage boost function of the center common leg, where the power source is connected to the mid node. The voltage boost ratio must be determined by the duty cycle of  $Q_3$  and  $Q_4$  to maintain the DC bus voltage at a Constant value even though the power source voltage varies.

Table 1. Comparison of basic features of circuit topology

|            | Conventional | Proposed circuit | Proposed           |  |
|------------|--------------|------------------|--------------------|--|
|            | Circuit      | topology         | circuit Topology   |  |
|            | topology     |                  | with voltage boost |  |
|            |              |                  | function           |  |
| Switching  | 8            | 7                | 6                  |  |
| devices    |              |                  |                    |  |
| counts     |              |                  |                    |  |
| Auxiliary  | 0            | Required         | Required           |  |
| devices    |              |                  |                    |  |
| Diode      | 8            | 7                | 7                  |  |
| Inductor   | 0            | 1                | 1                  |  |
| Efficiency | Highest      | Lowest           | Medium             |  |

Therefore, the duty cycles of  $Q_1$ ,  $Q_2$ ,  $Q_5$  and  $Q_6$  are also adjusted in accordance with the voltage boost ratio of the center leg. Table 1 shows the comparison of basic features of circuit topology.

#### 3. Operating Principle of the Proposed Chopper

#### (3.1) Proposed Three-Leg Full-Bridge Chopper

In this section, two basic operations of the proposed tree-leg full-bridge chopper are discussed. The first one is the case of a forward motion where both of the two DC motors are operated in the same direction to move the wheelchair forward. The second one is a backward motion where both of the two DC motors are operated in the same direction to move the wheelchair backward. Figure 4 shows the operating key waveform, operation modes and currents paths of the forward motion. Before analysing the operation of the circuit, several assumptions are employed;

- 1) All devices are ideal;
- 2) Constant switch duty cycle;
- 3) The electrical parameters of two DC motors are equal.

Where,  $V_{\rm S}$  is the input power supply voltage,  $V_{\rm ML}$  is the voltage at the left motor,  $V_{\rm MR}$  is the voltage at the right motor,  $I_{\rm ML}$  is the current at the left motor,  $I_{\rm MR}$  is the current at the right motor,  $D_{\rm S1}$ ,  $D_{\rm S2}$ ,  $D_{\rm S3}$ ,  $D_{\rm S4}$ ,  $D_{\rm S5}$  and  $D_{\rm S6}$  is the duty circle for  $Q_1$ ,  $Q_2$ ,  $Q_3$ ,  $Q_4$ ,  $Q_5$  and  $Q_6$ , respectively.  $T_{\rm S1}$ ,  $T_{\rm S2}$ ,  $T_{\rm S3}$ ,  $T_{\rm S4}$ ,  $T_{\rm S5}$  and  $T_{\rm S6}$  is the time period of switching frequency of  $Q_1$ ,  $Q_2$ ,  $Q_3$ ,  $Q_4$ ,  $Q_5$  and  $Q_6$ , respectively. Figure 4(a) shows the operating mode of the forward motion. The key operational waveforms of this mode are shown in Fig. 4(b).



Fig. 4. Forward operation (a) current paths (b) key operational waveforms







Fig. 5. Backward operation (a) current paths (b) key operational waveforms

1) Mode 1 ( $t_1$ - $t_2$ ,  $t_3$ - $t_4$ ,  $t_5$ - $t_6$  and  $t_7$ - $t_8$ ): The main switch (Q1,  $Q_4$  and  $Q_5$ ) are turned on  $Q_2$ ,  $Q_3$  and  $Q_6$ ) are turned off, the current from power source flows to the left and right motor to move wheelchair goes forward. Both current and voltage amplitude of two motors are positive.

2) Mode 2  $(t_0 - t_1, t_2 - t_3, t_4 - t_5, t_6 - t_7 \text{ and } t_8 - t_9)$ : The main switch  $Q_4$  is still turned on and  $(Q_1, Q_2, Q_3, Q_5 \text{ and } Q_6)$  are turned off.

The freewheeling effect is occurred.  $D_1$  and  $Q_3$  (for left motor)  $D_5$  and  $Q_3$  (for right motor) conduct the armature current and then the armature current beings to decrease until mode 1 is started again.

3) Mode  $3(t_9 \cdot t_{10}, t_{11} \cdot t_{12}, t_{13} \cdot t_{14}, t_{15} \cdot t_{16} \text{ and } t_{17} \cdot t_{18})$ : The main switch  $Q_4$  is turned on and  $(Q_1, Q_2, Q_3, Q_5 \text{ and } Q_6)$  are turned off. The freewheeling effect is occurred.  $D_2$  and  $Q_4$  (for left motor)  $D_6$  and  $Q_4$  (for right motor) conduct the armature current and then the armature current beings to decrease until mode 1 is started again.

4) Mode  $4(t_{10}-t_{11}, t_{12}-t_{13}, t_{14}-t_{15} and t_{16}-t_{17})$ :  $Q_4$  is still turned. on. This mode operation is similar to Mode 4 Fig. 5(a) shows the operating mode of backward motion. The key operational waveforms of this mode are illustrated in Fig. 5(b).

5) Mode 1 ( $t_1$ - $t_2$ ,  $t_3$ - $t_4$ ,  $t_5$ - $t_6$  and  $t_7$ - $t_8$ ): The main switch (Q<sub>2</sub>, Q<sub>3</sub> and Q<sub>6</sub>) are turned on, Q<sub>1</sub>, Q<sub>4</sub> and Q<sub>5</sub> are turned off, the current from power source flows to the left and right motor to move wheelchair goes backward. Both current and voltage amplitude of two motors are negative.

6) Mode 2  $(t_0 - t_1, t_2 - t_3, t_4 - t_5, t_6 - t_7 \text{ and } t_8 - t_9)$ : The main switch  $Q_3$  is still turned on and  $Q_1, Q_2, Q_4, Q_5$  and  $Q_6$  are turned off. The freewheeling effect is occurred.  $D_1$  and  $Q_3$  (for left motor)  $D_5$  and  $Q_3$  (for right motor) conducts the armature current and then the armature current beings to decrease until mode 1 is started again.

7) Mode 3 ( $t_9$ - $t_{10}$ ,  $t_{11}$ - $t_{12}$ ,  $t_{13}$ - $t_{14}$ ,  $t_{15}$ - $t_{16}$  and  $t_{17}$ - $t_{18}$ ): The main switching devices  $Q_2$ ,  $Q_4$  and  $Q_6$  are turned on. The armature current of left side motor flows in the loop consisted of  $L_a$ ,  $R_a$ ,  $D_2$  and  $Q_4$ . The armature current of left side motor flows in the loop consisted of  $L_a$ ,  $R_a$ ,  $D_6$  and  $Q_4$ .

8) Mode 4 ( $t_{10}$ - $t_{11}$ ,  $t_{12}$ - $t_{13}$ ,  $t_{14}$ - $t_{15}$  and  $t_{16}$ - $t_{17}$ ): The main switch  $Q_4$  is still turned on and  $Q_1$ ,  $Q_2$ ,  $Q_3$ ,  $Q_5$  and  $Q_6$  are turned off. Although Q1 and  $Q_5$  are off, the operation of this mode is similar to Mode 4.

Besides two modes, there are the other modes operations as shows in table 2. Only two basics mode operating are deeply discussed because its can cover of all modes. For example, in pivot left turn operation, the left side motor is operated for backward motion but the right side motor is operated for forward motion. The result is, the wheelchair moves around its in counter-clockwise direction.

In the table 1, it is shown that the proposed circuit is capable of producing positive or negative voltages across the DC motor, whilst delivering current to the motor in either direction. The disadvantage point of this topology is occurred in pivot operation. Because of the switching operation of  $Q_3$  and  $Q_4$  is complementary with a 50-% duty cycle. It is called "Time Sharing Technique". There for, the output voltage of this chopper will be half of the inherent rated value. The left or right turn mode operational condition is to operate only one motor. However, in order to obtain smooth turning operation, both of two motor much be operated as the same direction but one of each other is operate by lower speed than each one.

| Mode                    | Condition   | (Left motor voltage) $\overline{V}_{ML}$      |   | (Right motor voltage) $\overline{V}_{\scriptscriptstyle M\!R}$ |   |
|-------------------------|---|---|---|--|---|
|                         |   | Proposed chopper                              | Proposed chopper with boost<br>function   | Proposed chopper   | Proposed chopper with boost<br>function   |
| Stop                    | $V_{\rm ML}=V_{\rm MR}=0$                               | 0   | 0   | 0  | 0   |
| Forward                 | $+V_{\scriptscriptstyle ML}=+V_{\scriptscriptstyle MR}$ | $D_{S1}D_{S4}V_B$                             | $D_{S1}D_{S4} \frac{V_B}{(1-D_{S4})}$   | $D_{SS}D_{S4}V_B$  | $D_{S5}D_{S4} \frac{V_B}{(1 - D_{S4})}$   |
| Backward                | $-V_{ML} = -V_{MR}$                                     | $-D_{S2}D_{S3}V_B$                            | $-D_{S2}V_B$  | $-D_{S6}D_{S3}V_B$   | $-D_{S6}V_B$  |
| Pivot left turn         | $-V_{ML},+V_{MR}$                                       | $-D_{S2}D_{S3}V_B$                            | $-D_{S2}V_B$  | $D_{S5}D_{S4}V_B$  | $D_{S5}D_{S4}\frac{V_B}{\left(1-D_{S4}\right)}$   |
| Pivot right turn        | $+V_{ML},-V_{MR}$                                       | $D_{S1}D_{S4}V_B$                             | $D_{S1}D_{S4} \frac{V_B}{(1 - D_{S4})}$   | $-D_{S6}D_{S3}V_B$   | $-D_{S6}V_B$  |
| Left<br>turn(Forward)   | $0 \leq + V_{ML} < + V_{MR}$                            | $0 \le D_{S1} D_{S4} V_B < D_{S5} D_{S4} V_B$ | $0 \le D_{S1} D_{S4} \frac{V_B}{(1 - D_{S4})} < D_{S5} D_{S4} \frac{V_B}{(1 - D_{S4})}$ | $D_{S5}D_{S4}V_B$  | $D_{S5}D_{S4}\frac{V_B}{\left(1-D_{S4}\right)}$   |
| Right<br>turn(Forward)  | $0 \leq +V_{MR} < +V_{ML}$                              | $D_{S1}D_{S4}V_B$                             | $D_{S1}D_{S4}rac{V_B}{(1-D_{S4})}$   | $0 \le D_{SS} D_{S4} V_B < D_{S1} D_{S4} V_B$                  | $0 \le D_{SS} D_{S4} \frac{V_B}{(1 - D_{S4})} < D_{S1} D_{S4} \frac{V_B}{(1 - D_{S4})}$ |
| Left<br>turn(Backward)  | $-V_{MR} < -V_{ML} \leq 0$                              | $-D_{S6}D_{S3}V_B < -D_{S2}D_{S3}V_B \leq 0$  | $-D_{S6}V_B < -D_{S2}V_B \leq 0$  | $-D_{S6}D_{S3}V_B$   | $-D_{S6}V_B$  |
| Right<br>turn(Backward) | $-V_{ML} < -V_{MR} \le 0$                               | $-D_{S2}D_{S3}V_B$                            | $-D_{S2}V_B$  | $-D_{S2}D_{S3}V_B < -D_{S6}D_{S3}V_B \le 0$                    | $-D_{S2}V_B < -D_{S6} V_B \le 0$  |

Table 2. Summarize of all operational modes condition

# (3.2) Proposed Three-Leg Full-Bridge Chopper With Voltage Boost Function

This section describes the proposed tree-leg full-bridge chopper with voltage boost function. The two basic operation modes are discussed. The first one is the forward motion and the second one is the backward motion. The basic operation is similar to the proposed circuit in previous section but this circuit topology is incorporated voltage boost circuit. The main equivalent operation modes of forward motion are shown in Fig. 6, and described as follows.

1) Mode 1  $(t_0 \cdot t_1)$ : The main switch  $Q_4$  is turned on while  $Q_1$ ,  $Q_2$ ,  $Q_3$ ,  $Q_5$  and  $Q_6$  are off. The inductor current increases linearity with a slope  $V_{\rm S}/L_{\rm B}$ . The inductor current flows in the loop consisted of  $V_{\rm S}$ ,  $L_{\rm B}$ ,  $D_{\rm B}$  and  $Q_4$ .

2) Mode 2 ( $t_1$ - $t_2$ ,  $t_3$ - $t_4$ ,  $t_5$ - $t_6$  and  $t_7$ - $t_8$ ): The main switch  $Q_1$ ,  $Q_4$  and  $Q_5$  are turned on,  $Q_2$ ,  $Q_3$  and  $Q_6$  are turned off, the current from capacitor C flows to the left and right motor to move wheelchair goes forward. The switching operation of  $Q_4$  allows voltage boost action and provides current flows through the two DC motors at the same time. Both current and voltage amplitude of two motors are positive.

3) Mode 3 ( $t_2$ - $t_3$ ,  $t_4$ - $t_5$ ,  $t_6$ - $t_7$  and  $t_8$ - $t_9$ ): The main switch  $Q_4$  is still turned on and  $Q_1$ ,  $Q_2$ ,  $Q_3$ ,  $Q_5$  and  $Q_6$  are turned off. The freewheeling effect is occurred. The switching operation of  $Q_4$  is on for voltage boost action which is similar to Mode 1.

4) Mode 4  $(t_9 \cdot t_{10}, t_{11} \cdot t_{12}, t_{13} \cdot t_{14}, t_{15} \cdot t_{16} \text{ and } t_{17} \cdot t_{18})$ : The main switching devices  $Q_2$ ,  $Q_3$  and  $Q_6$  are turned on. The inductor  $L_B$  acts as a current source and continues to charge the capacitor C through  $D_3$ . At the same time, the armature current of left side motor flows in the loop consisted of  $L_a$ ,  $R_a$ ,  $D_1$  and  $Q_3$ . The armature current of left side motor flows in the loop  $Q_3$ .

5) Mode 5 ( $t_{10}$ - $t_{11}$ ,  $t_{12}$ - $t_{13}$ ,  $t_{14}$ - $t_{15}$  and  $t_{16}$ - $t_{17}$ ): The main switch  $Q_3$  is still turned on and  $Q_1$ ,  $Q_2$ ,  $Q_4$ ,  $Q_5$  and  $Q_6$  are turned off. Although Q1 and  $Q_5$  are off, the operation of this mode is similar to Mode 4.

The average voltage of the left and right side motor are determined by equation in the table 1. It is shown that the circuit has capable to boost voltage even though the power source voltage varies.





Fig. 7. Backward operation (a) current paths (b) key operational waveforms

| Voltage of power supply                    | $24~\mathrm{V}$   |
|--|-------------------|
| Switching frequency $(Q_1, Q_2, Q_5, Q_6)$ | 10 kHz            |
| Switching frequency $(Q_3, Q_4)$           | 1 kHz             |
| Capacitor C                                | 3600uF, 350 V     |
| Rated power of DC motors                   | 60 W              |
| Rated voltage of DC motors                 | 24 V              |
| Inductor $L_{\rm B}$                       | $0.5 \mathrm{mH}$ |

Table 3. Electrical parameters of prototype

Fig. 5(a) shows the operating mode of backward motion. The operating key wave form of this mode is illustrated in Fig. 5(b).

6) Mode 1 ( $t_0$ - $t_1$ ): The main switch  $Q_4$  is turned on while  $Q_1$ ,  $Q_2$ ,  $Q_3$ ,  $Q_5$  and  $Q_6$  are off. The inductor current increases linearity with a slope  $V_S/L_B$ .

7) Mode 2  $(t_1 - t_2, t_3 - t_4, t_5 - t_6 \text{ and } t_7 - t_8)$ : The main switch  $Q_2$ ,  $Q_3$  and  $Q_6$  are turned on,  $Q_1$ ,  $Q_4$  and  $Q_5$  are turned off, the current from negative pole of capacitor C flows to the left and right motor to move wheelchair goes backward. Both current and voltage amplitude of two motors are negative.

8) Mode 3 ( $t_2$ · $t_3$ ,  $t_4$ · $t_5$ ,  $t_6$ · $t_7$  and  $t_8$ · $t_9$ ): The main switch  $Q_3$  is still turned on and  $Q_1$ ,  $Q_2$ ,  $Q_4$ ,  $Q_5$  and  $Q_6$  are turned off. The freewheeling effect is occurred. This mode is similar to Mode 4 of forward operation.

9) Mode 4  $(t_5 \cdot t_{10}, t_{11} \cdot t_{12}, t_{13} \cdot t_{14}, t_{15} \cdot t_{16} and t_{17} \cdot t_{18})$ : The main switching devices  $Q_2$ ,  $Q_4$  and  $Q_6$  are turned on. The inductor current increases linearity with a slope  $V_S/L_B$ . At the same time, the armature current of left side motor flows in the loop consisted of  $L_a$ ,  $R_a$ ,  $D_2$  and  $Q_4$ . The armature current of left side motor flows in the loop consisted of  $L_a$ ,  $R_a$ ,  $D_2$  and  $Q_4$ .

10) Mode 5 ( $t_{10}$ - $t_{11}$ ,  $t_{12}$ - $t_{13}$ ,  $t_{14}$ - $t_{15}$  and  $t_{16}$ - $t_{17}$ ): The main switch  $Q_4$  is still turned on and  $Q_1$ ,  $Q_2$ ,  $Q_3$ ,  $Q_5$  and  $Q_6$  are turned off. Although Q1 and  $Q_5$  are off, the operation of this mode is similar to Mode 4.

The same as the previously circuit topology, there are the other modes as shown in table 2. It is shown that the two proposed topologies are capable of producing positive or negative voltages across the DC motor, whilst delivering current to the motor in either direction.

#### 4. Computer Simulation and Experimental Results

In order to verify the theoretical analysis and design of the previous sections, simulations and experiments have been done. The parameters used are listed in Table 3.

**4.1 Simulation Results** Fig. 8(a) shows the simulated waveforms of forward motion.  $Q_1$  and  $Q_5$  are operated at 10 kHz and  $Q_4$  at 1 kHz with 50-% duty cycle. Fig. 8 (b) illustrates the simulated waveforms in backward motion,  $Q_2$  and  $Q_6$  are operated at 10 kHz and  $Q_4$  at 1 kHz with 50-% duty cycle. For both of output current of forward and backward motion, they show those continuous current modes are achieved during on time period of  $Q_4$  and  $Q_3$ , respectively. Fig. 9(a) and (b) show the simulated waveform of the proposed chopper with voltage boost function for forward and backward operation, respectively.

**4.2 Experimental Results** Fig. 10 (a) and (b) show the experimental waveforms of proposed chopper circuit. Fig. 10(a) illustrates the gate signal of  $Q_1$  and  $Q_4$ , voltage and current waveforms of left side motor in forward motion. Fig. 10(b) illustrates the gate signals of  $Q_2$  and  $Q_3$ , voltage and current waveforms of left side motor in forward motion. The experimental implementation of the proposed chopper with voltage boost function will be conducted in future work.



Fig. 8. Simulated waveforms of proposed chopper (a) Forward motion (b) Backward motion







Fig. 9. Simulated waveforms of proposed chopper with voltage boost function (a) Forward motion(b) Backward motion



Fig. 10. Experimental waveforms of proposed chopper (a) Forward motion (b) Backward motion

It can be seen that the simulated and experimental results are in close agreement with the above theoretical analysis.

## 5. Conclusion

In this paper, the new DC chopper to drive independent two DC motors was proposed. The proposed power circuit consists of three-leg full-bridge chopper, which has advantage over conventional circuit configuration in the reduced counts of the switching devices. In addition, the proposed three-leg configuration incorporates the voltage boost function of the power source. This function compensates for the reduced voltages applied to the motors. This circuit configuration can be applied to not only electric wheelchairs but also other traction systems that require multiple pairs of DC motors.

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